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JOURNAL OF SOLID STATE CHEMISTRY

Journal of Solid State Chemistry 179 (2006) 3672-3680

www.elsevier.com/locate/jssc

# Synthesis, crystal structure and magnetic properties of new indium rhenium and scandium rhenium oxides, In<sub>6</sub>ReO<sub>12</sub> and Sc<sub>6</sub>ReO<sub>12</sub>

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Received 11 May 2006; received in revised form 25 July 2006; accepted 29 July 2006 Available online 4 August 2006

#### Abstract

The new complex indium rhenium and scandium rhenium oxides,  $In_6ReO_{12}$  and  $Sc_6ReO_{12}$ , have been synthesized as single phases in sealed silica tubes and by high-pressure high-temperature syntheses, and their crystal structures have been determined by single crystal X-ray diffraction. The compounds crystallize in a rhombohedral structure related to the distorted fluorite structure like  $Ln_6ReO_{12}$  for some rare earth elements, S. G.: *R*-3, *Z* = 3, *a*<sub>H</sub> = 9.248(2) Å, *c*<sub>H</sub> = 8.720(2) Å for  $Sc_6ReO_{12}$  and *a*<sub>H</sub> = 9.492(1) Å, *c*<sub>H</sub> = 8.933(1) Å for  $In_6ReO_{12}$ . A maximum in magnetization is observed for  $Sc_6ReO_{12}$  at  $T(M_{max}) = 1.89(2)$  K, whereas ferromagnetic ordering is found for  $In_6ReO_{12}$  by a pronounced increase in the temperature dependence of magnetization at  $T_C = 7.5(5)$  K. The magnetic moment per rhenium ion in  $In_6ReO_{12}$  and  $Sc_6ReO_{12}$  is 0.84(1) and 0.65(1)  $\mu_B$ , respectively, derived from the paramagnetic regions.  $\bigcirc$  2006 Elsevier Inc. All rights reserved.

PACS: 61.66.Fn

Keywords: Indium rhenium oxide In<sub>6</sub>ReO<sub>12</sub>; Scandium rhenium oxide Sc<sub>6</sub>ReO<sub>12</sub>; Distorted fluorite structure; Magnetism of Re<sup>+6</sup>

## 1. Introduction

 $Ln_6$ MeO<sub>12</sub> compounds, crystallizing in space group *R*-3 with a distorted fluorite-type structure, are known in the MeO<sub>3</sub>- $Ln_2$ O<sub>3</sub> system, where *Me*-Mo, W, Re or *U*, and *Ln*-some rare earth elements [1–3]. The same structure is adopted by some ordered Ln<sub>7</sub>O<sub>12</sub> phases (*Ln* = Ce, Pr, Tb) [2]. These authors have proposed a critical ratio between the ionic radii of the hexavalent metal ions and the trivalent rare earth ion to be equal about 0.67 or more as an empirical criterion for the formation of the *Ln*<sub>6</sub>MeO<sub>12</sub> phases with a rhombohedral structure for *Me* = Mo, W, U. But some Ln<sub>6</sub>ReO<sub>12</sub> phases with this rhombohedral structure exist [3], where the ionic radii ratio Re<sup>+6</sup>/*Ln*<sup>3+</sup> is smaller than for the molybdates, tungstates and uranates, for example, Ho<sub>6</sub>ReO<sub>12</sub> with  $r(\text{Re}^{+6})/r(\text{Ho}^{+3}) = 0.61$  [4]. In a previous work [3] the synthesis and investigation of magnetism of  $Ln_6 \text{ReO}_{12}$  compounds (Ln = Ho, Er, Tm, Yb and Lu) were presented. Rhenates of rare earth elements show different magnetic properties depending on the rare earth ion, a magnetic moment of  $0.74 \,\mu_B$  per Re<sup>+6</sup> was deduced for Lu<sub>6</sub>ReO<sub>12</sub> (Lu<sup>3+</sup> itself is diamagnetic).

Sc- and In-containing rhombohedral phases  $Sc_6MoO_{12}$ ,  $Sc_6WO_{12}$  [5,6] and  $In_6WO_{12}$  [7,8] are also known. The  $Sc^{3+}$  and  $In^{3+}$  ions resemble heavy rare earth ions in different compounds despite of their smaller ionic radii [9]. In the systems Sc-Re-O and In-Re-O only perrhenates  $Sc(ReO_4)_3$  and  $In(ReO_4)_3$  are known [5,10,11], and the crystal structure of  $Sc(ReO_4)_3 \cdot 3H_2O$  [12] and In  $(ReO_4)_3 \cdot 4.5H_2O$  [13] were determined. In this work we report the synthesis of  $Sc_6ReO_{12}$  by two different methods, in a sealed silica tube and by a high pressure high temperature (HPHT) method, the synthesis of  $In_6ReO_{12}$  by a high-pressure high-temperature method, the structure determination by single-crystal X-ray diffraction, and an investigation of magnetic properties of these compounds.

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<sup>0022-4596/\$ -</sup> see front matter  $\odot$  2006 Elsevier Inc. All rights reserved. doi:10.1016/j.jssc.2006.07.041

### 2. Experimental

One- and two-temperature syntheses in sealed silica tubes. Samples of nominal composition Sc<sub>6</sub>ReO<sub>12</sub> were synthesized in sealed silica tubes using Sc<sub>2</sub>O<sub>3</sub> (Strem Chemicals, 99.99%) and ReO<sub>3</sub> (Strem Chemicals, 99.9%) or Re (Alfa Aesar, 99.997%) and Re<sub>2</sub>O<sub>7</sub> (Alfa Aesar, 99.9%) as starting materials. A stoichiometric mixture of Sc<sub>2</sub>O<sub>3</sub> and ReO<sub>3</sub> was ground in an agate mortar under acetone and pressed into pellets, which were placed in an Al<sub>2</sub>O<sub>3</sub> crucible, sealed in an evacuated silica tube (ordinary optical grad, water content 30 ppm), and annealed in a muffle furnace. In a two-temperature synthesis two pellets of Sc<sub>2</sub>O<sub>3</sub> and ReO<sub>3</sub> mixture in two crucibles were divided from each other by a small quartz stick and placed in a silica tube. The tube was evacuated and placed into a tube furnace with a temperature gradient. Before use, Sc<sub>2</sub>O<sub>3</sub> and ReO<sub>3</sub> were dried in air at 110–115 °C for 2–3 h, silica tubes and Al<sub>2</sub>O<sub>3</sub> crucibles were dried in the oxypropane flame. If Re and Re<sub>2</sub>O<sub>7</sub> were used as Re source, a powder mixture of Re,  $Sc_2O_3$  and  $Re_2O_7$  oxides in the molar ratio 1:21:3 was placed within a glove box into a silica tube using an Al<sub>2</sub>O<sub>3</sub> crucible. The tube was sealed under vacuum.

*High-pressure high-temperature synthesis*: A high-pressure synthesis of  $In_6ReO_{12}$  and  $Sc_6ReO_{12}$  was performed in a Girdle-Belt apparatus with pyrophyllite as the pressure-transmitting medium. A graphite furnace and a platinum capsule containing the reactants were used for the

experiment. A mixture of  $In_2O_3$  (Alfa Aesar, 99.99%) and ReO<sub>3</sub> (Strem Chemicals, 99.9%) in molar ratio In:Re = 6:1 or a mixture of one mole of  $Sc_2O_3$ , one mole of ReO<sub>2</sub> (Alfa Aesar, 99.9%) and one mole of ReO<sub>3</sub> with nominal composition "ScReO<sub>4</sub>" was ground in an agate mortar under acetone and filled in a platinum capsule. The sample holder was pressed up to 50 kbar before the temperature was raised to 1300 °C with a rate of 50°/min. The heating current was switched off after 120 min and after cooling to room temperature, pressure was released.

Single-crystal X-ray diffraction: The crystal structure of  $In_6ReO_{12}$  and  $Sc_6ReO_{12}$  was solved by single-crystal X-ray diffraction using the Xcalibur system from Oxford Diffraction. The software packages SHELXS [14] and SHELXL [15] were used for structure solution and refinement as included in X-STEP32 [16]. A combined empirical absorption correction with frame scaling was applied, using the scale3 abspack command in CrysalisRed [17].

X-ray *powder diffraction (XPD)*. Phase analysis and determination of cell parameters were carried out using X-ray powder diffraction with a STOE STADI P diffractometer (Mo- $K\alpha_1$ -radiation,  $\lambda = 0.7093$  Å) in steps of 0.02° for 2 $\Theta$  from 3 to 45° in transmission mode. All diffraction patterns have been analyzed by full-profile Rietveld refinements, using the software package WinPLOTR [18].

Thermogravimetry (TG). The Re content in the Sc<sub>6</sub>ReO<sub>12</sub> samples was determined by thermogravimetric

Table 1 Conditions and results of (a)one-temperature syntheses and (b) two-temperature synthesis of  $Sc_6ReO_{12}$ 

No.	Starting materials	<i>T</i> (°C)	Time (h)	Products (wt%)	Cell parameters of Sc <sub>6</sub> ReO <sub>12</sub> (Å)
(a)					
1	$Sc_2O_3 + ReO_3$ (" $Sc_6ReO_{12}$ ")	950	18	$Sc_2O_3$ -90%, 10%- unknown phase	
2	$\frac{\text{Re} + \text{Sc}_2\text{O}_3 + \text{Re}_2\text{O}_7}{(\text{``Sc}_6\text{ReO}_{12}\text{''})}$	1000	41	$Sc_6ReO_{12}$ -43% $Sc_2O_3$ -52%,	a = 9.2463(2), c = 8.7119(2)
3	$\frac{\text{Sc}_2\text{O}_3 + \text{ReO}_3}{(\text{``Sc}_6\text{ReO}_{12}\text{''})}$	1010	33	$S_{0}^{-4}$ -unknown phase $Sc_{6}ReO_{12}$ -50% $Sc_{2}O_{3}$ -46% $R_{2}O_{2}$ -4%	a = 9.2444(3), c = 8.7126(3)
4	$\frac{\mathrm{Sc_2O_3}+\mathrm{ReO_3}}{(\mathrm{``Sc_6ReO_{12}''})}$	1050	16	$c_{c_{12}-4\%}$ Sc <sub>6</sub> ReO <sub>12</sub> -57% Sc <sub>2</sub> O <sub>3</sub> -37%, ReO-6%	a = 9.2450(2), c = 8.7123(3)
5	$Sc_2O_3 + ReO_3$ (" $Sc_6ReO_{12}$ ")	1080	50	$Sc_{6}ReO_{12}-7\%$ $Sc_{2}O_{3}-85\%$ , $ReO_{2}-6\%$ 2%unknown phase	a = 9.251(1), c = 8.718(1)
(b)				270 unknown phuse	
1	$Sc_2O_3 + ReO_3$ (" $Sc_6ReO_{12}$ ")	$T_2 = 1010$ $T_1 = 1020$	33	$Sc_6ReO_{12}$ -100% $Sc_6ReO_{12}$ -91%	a = 9.2451(2), c = 8.7148(2)
	$\frac{\text{Sc}_2\text{O}_3 + \text{ReO}_3}{(\text{``Sc}_6\text{ReO}_{12}\text{''})}$			Sc <sub>2</sub> O <sub>3</sub> -9%	a = 9.2455(1), c = 8.7141(2)Å
2	$Sc_2O_3 + ReO_3$ (" $Sc_6ReO_{12}$ ") $Sc_2O_3 + ReO_3$	$T_2 = 1025$ $T_1 = 1035$	91	$\frac{Sc_{6}ReO_{12}-72\%}{Sc_{2}O_{3}-28\%}$	a = 9.2478(1), c = 8.7178(2)
	$("Sc_6ReO_{12}")$	-		$Sc_6ReO_{12}-50\%$ $Sc_2O_3-45\%$ + 5% unknown phase	a = 9.2479(3), c = 8.7168(4)

measurements. The method is based on the ability of Re in a number of complex oxides to be oxidized to volatile  $Re_2O_7$  by heating in air. Samples were carefully weighed in  $Al_2O_3$  crucibles before and after annealing in air at 950 °C during 24 h. The Re content in the samples was estimated assuming that the mass loss corresponds to  $ReO_3$  oxide. The phase composition of the residue (Sc<sub>2</sub>O<sub>3</sub>) was always checked by X-ray diffraction.

*Magnetic susceptibility.* The magnetic properties of  $In_6ReO_{12}$  and  $Sc_6ReO_{12}$  have been studied with a superconducting quantum interference device (SQUID) from Quantum Design. Measurements were performed upon heating in the temperature range from 1.7 to 300 K and with an applied field strength of 500 G, both in field-cooled (FC) and zero-field cooled (ZFC) mode.

#### 3. Results and discussion

#### 3.1. Synthesis and characterization of Sc<sub>6</sub>ReO<sub>12</sub> samples

# 3.1.1. One- and two-temperature synthesis in a sealed silica tube

Conditions and results of one-temperature  $Sc_6ReO_{12}$ synthesis in a sealed silica tube are presented in Table 1(a). The amount of  $Sc_6ReO_{12}$  phase in the products changes with increasing synthesis temperature from 950 to 1080 °C. No  $Sc_6ReO_{12}$  was found in reaction products after synthesis at 950 °C, and the maximal  $Sc_6ReO_{12}$  content was found after synthesis at 1050 °C.  $Sc_2O_3$  and  $ReO_2$  were always detected as admixtures in the syntheses. This can be explained by taking into account some reaction, which takes place in the silica tube at high temperatures. Rhenium(VI) oxide  $ReO_3$  is not stable under heating and decomposes at 630 °C into  $ReO_2$  and  $Re_2O_7$  [19] according to

$$3\text{ReO}_3(s) \Rightarrow \text{ReO}_2(s) + \text{Re}_2\text{O}_7(g). \tag{1}$$

The reaction with  $Sc_2O_3$  occurs partly through the gas phase:

$$9Sc_2O_3(s) + ReO_2(s) + Re_2O_7(g) \Leftrightarrow 3Sc_6ReO_{12}(s).$$
(2)

The estimated value of  $\text{Re}_2\text{O}_7$  pressure inside the silica tube during the synthesis at 1050 °C was about 0.3 atm. For this estimation a pellet of the reacting mixture was weighed before the synthesis and after quenching the tube into water from synthesis temperature. It is assumed that the mass difference of the pellet corresponds to  $\text{Re}_2\text{O}_7$ evaporation.

In order to facilitate the formation of the  $Sc_6ReO_{12}$ phase according to reaction (2), the  $Re_2O_7$  partial pressure must be higher than the equilibrium value [20]. We have performed some experiments with a fixed  $Re_2O_7$  pressure in a reaction tube applying two-temperature synthesis as described in [21,22], in which complex oxides containing Hg had been prepared. At higher temperature  $T_1$  a mixture of  $Sc_6ReO_{12}$ ,  $Sc_2O_3$  and  $ReO_2$  was used to adjust the  $Re_2O_7$ partial pressure in the tube, whereas in the lowertemperature region single phase Sc<sub>6</sub>ReO<sub>12</sub> must be formed, because the  $Re_2O_7$  pressure in the tube is higher than the one at  $T_2 < T_1$ . The use of the two-temperature method in a sealed tube gives good results if the synthesis time is about 30-40 h (experiment 1, Table 1b and Fig. 1(a)). If the synthesis was performed during 90 h or more, the  $Sc_6ReO_{12}$ amount in the products reduced to 70% and Sc<sub>2</sub>O<sub>3</sub> was found as an impurity (experiment 2, Table 1b). In this case a lot of small black shining ReO<sub>2</sub> crystals were found on the walls of the coldest part of the tube. It is known that in the system Re-O at 800-1000 °C ReO2 crystals can be easily grown during some days by means of chemical transport reactions with water molecules as a transport agent [23]. The author of [23] noted, that water traces in an ordinary silica glass are enough for the ReO<sub>2</sub> transport. Therefore, due to Re transport in form of ReO<sub>2</sub>, its content in samples decreases and Sc<sub>2</sub>O<sub>3</sub> appears as a second phase. The synthesis time must be reduced to 20–30 h in order to avoid loss of ReO<sub>2</sub>.



Fig. 1. The observed and fitted profiles together with the corresponding difference curve (Mo- $K\alpha_1$ ): (a) for Sc<sub>6</sub>ReO<sub>12</sub> obtained by two-temperature synthesis and (b) for In<sub>6</sub>ReO<sub>12</sub> obtained by high-pressure high-temperature synthesis. The reflection marks at the bottom belong to the monoclinic phase ReO<sub>2</sub>, 0.5 wt% and 1.5 wt% in Sc<sub>6</sub>ReO<sub>12</sub> and In<sub>6</sub>ReO<sub>12</sub> samples, respectively.

Note that the syntheses of  $Ln_6\text{ReO}_{12}$  (Ln = Ho, Er, Tm, Yb and Lu) phases at 1200 °C in Pt/Rh-tubes were always accompanied by forming of  $Ln_3\text{ReO}_8$  as impurity and never ReO<sub>2</sub>, which could be due to thermal decomposition of ReO<sub>2</sub> [19] according to

$$7\text{ReO}_2(s) = 3\text{Re}(s) + 2\text{Re}_2\text{O}_7(g).$$
 (3)

and the stability of  $Ln_3\text{ReO}_8$  phases in the system  $Ln_2\text{O}_3-\text{Re}_2\text{O}_7$  [24,25] at this temperature. Scandium perrhenate Sc(ReO<sub>4</sub>)<sub>3</sub> is not stable above 735 °C and decomposes to Re<sub>2</sub>O<sub>7</sub>(g) and Sc<sub>2</sub>O<sub>3</sub>. The compound Sc<sub>3</sub>ReO<sub>8</sub> is not known [5].

In all samples the Sc<sub>6</sub>ReO<sub>12</sub> phase appears as small dark grey crystals with a size up to 0.05–0.1 mm. The compound is stable in air at least for 1 month. The diffractogram of single phase Sc<sub>6</sub>ReO<sub>12</sub>, prepared by the two-temperature synthesis, is presented in Fig. 1(a). All reflections were explained based on a rombohedral unit cell with lattice parameters a = 9.25 Å and c = 8.72 Å. According to the thermogravimetric measurements the sample contains 63.7 wt% Sc<sub>2</sub>O<sub>3</sub>, which corresponds to the chemical composition Sc<sub>6</sub>ReO<sub>12</sub>.

#### 3.1.2. High-pressure high-temperature synthesis

The formation of  $Sc_6ReO_{12}$  crystals is also observed under high pressure up to 50 kbar and temperature up to 1300 °C. According to X-ray diffraction the sample with nominal composition " $Sc_2Re_2O_8$ " contained after synthesis 49 wt%  $Sc_6ReO_{12}$  and 51 wt%  $ReO_2$ . All reflections which do not belong to  $ReO_2$  were explained based on a rhombohedral unit cell with lattice parameters a = 9.2451(2) Å and c = 8.6988(3) Å. Note, that the sample obtained in absence of the gas phase (HPHT synthesis) has a smaller "c" parameter at the same "a" parameter in comparison with the sample prepared in the quartz tube at lower temperature (Table 1b, a = 9.2451(2) Å and c = 8.7148(2) Å).

#### 3.2. Synthesis and characterization of $In_6ReO_{12}$ samples

 $In_6ReO_{12}$  was successfully synthesized by high-pressure high-temperature synthesis only, attempts to prepare  $In_6ReO_{12}$  samples in a sealed silica tube led to formation of  $ReO_2$  and  $In(ReO_4)_3 \cdot 4.5H_2O$  as reaction products according to X-ray diffraction at ambient conditions. The

Table 2

Details of X-ray single-crystal data collection and structure refinement of Sc<sub>6</sub>ReO<sub>12</sub> and In<sub>6</sub>ReO<sub>12</sub>.

Crystal data		
Chemical formula	Sc <sub>6</sub> ReO <sub>12</sub>	$In_6ReO_{12}$
Formula weight	647.96	1067.12
Crystal system	Rhombohedral	Rhombohedral
Space group	R -3 (no. 148)	<i>R</i> -3 (no. 148)
Unit cell dimensions		
Hexagonal axes	$a_H = 9.248(2) \text{ Å}$	$a_H = 9.492(1) \text{ Å}$
-	$c_H = 8.720(2) \text{ Å}$	$c_H = 8.933(1) \text{ Å}$
Rhombohedral axes	$a_R = 5.836(3) \text{ Å}$	$a_R = 5.985(2) \text{ Å}$
	$\alpha = 97.35(1) \text{ Å}$	$\alpha = 97.397(6) \text{ Å}$
Cell volume	645.87(20) Å <sup>3</sup>	697.02(13)Å <sup>3</sup>
Ζ	3	3
Calculated density (g/cm <sup>3</sup> )	4.997	7.627
Radiation type	Mo-K $\alpha$ , $\lambda = 0.71073 \text{ Å}$	Mo- $K\alpha$ , $\lambda = 0.71073$ Å
No. of reflections for cell parameters	372	1215
Temperature (K)	293(2)	293(2)
Crystal form, colour	Prismatic, black	Prismatic, black
Crystal size (mm <sup>3</sup> )	0.050 0.030 0.020	$0.050 \cdot 0.045 \cdot 0.045$
Data collection		
Diffractometer	Oxford Diffraction Xcalibur; single-crystal X-ray	diffractometer with sapphire CCD detector
Data collection method	Rotation method data acquisition using $\omega$ and $\varphi$	scans(s)
Absorption coefficient	$18.510 \mathrm{mm}^{-1}$	$27.662 \mathrm{mm^{-1}}$
F(000)	891	1395
Range for data collection	3.45 to 29.78°	3.37 to 36.65°
Range of h, k, l	$-12 \le h \le 12, -11 \le k \le 12, -11 \le l \le 10$	$-13 \le h \le 13, -13 \le k \le 15, 14 \le l \le 14$
D (min), $d$ (max) for cell determination (Å)	0.737, 5.93	0.60, 6.1
Reflections collected/unique	1007/963	2203/755
Completeness to $\theta = 26.35^{\circ} (36.65^{\circ})$	0.921	0.975
Refinement method	Full-matrix least-squares on F <sup>2</sup>	
Data/restraints/parameters	963/0/31	755/0/31
Goodness-of-fit on $F^2$	1.106	1.107
Final R indices $[I > 2 \text{sigma}(I)]$	$R_1 = 0.0530, wR_2 = 0.1414$	$R_1 = 0.0224, wR_2 = 0.0546$
R indices (all data)	$R_1 = 0.0595, wR_2 = 0.1588$	$R_1 = 0.0267, wR_2 = 0.0555$
Largest diff. peak and hole	$3.16, -2.59 \text{ e/} \text{\AA}^3$	$2.031, -1.622 \text{ e/Å}^3$

presence of water molecules in indium perrhenate must be due to exposure of the sample to air during X-ray diffraction for some hours; it is known that the most of perrhenates of two- and three-valent metals are stable in air only in the form of hydrates [12,13]. The initial compound  $In_2O_3$  was always observed. The diffractogram of  $In_6ReO_{12}$ is shown in Fig. 1(b). Almost all reflections were explained based on a rhombohedral unit cell with lattice parameters a = 9.4658(2)Å, c = 8.9136(2)Å (in hexagonal setting), except one peak at  $2\theta = 12^{\circ}$  which belongs to monoclinic ReO<sub>2</sub> (1.5 wt%).

# 3.3. Structural features of In<sub>6</sub>ReO<sub>12</sub> and Sc<sub>6</sub>ReO<sub>12</sub>

According to X-ray structure analysis of In<sub>6</sub>ReO<sub>12</sub> single crystals and twinned Sc<sub>6</sub>ReO<sub>12</sub> crystals, the compounds crystallize in a distorted anion-deficient fluorite-type structure with formally six oxygen vacancies per one cell on the threefold axes like some  $Ln_6MO_{12}$  compounds where Ln is some rare earth element and M = Mo, W, Re or U (space group R-3, a = 9.492(1) Å, c = 8.933(1) Å for In<sub>6</sub>ReO<sub>12</sub> and a = 9.248(2) Å, c = 8.720(2) Å for Sc<sub>6</sub>ReO<sub>12</sub> (Table 2).

In the case of  $Sc_6ReO_{12}$  all observed reflections can only be indexed based on a 2-domain crystal. The orientations of the two domains with respect to each other are given by the following relations:

$$a_{1}^{*} = -17/21 \cdot a_{2}^{*} + 8/21 \cdot b_{2}^{*} - 16/21 \cdot c_{2}^{*},$$
  

$$b_{1}^{*} = 5/21 \cdot a_{2}^{*} - 11/21 \cdot b_{2}^{*} - 20/21 \cdot c_{2}^{*},$$
  

$$c_{1}^{*} = -1/3 \cdot a_{2}^{*} - 2/3 \cdot b_{2}^{*} + 1/3 \cdot c_{2}^{*}$$
  
or vice versa  

$$a_{2}^{*} = -17/21 \cdot a_{1}^{*} + 8/21 \cdot b_{1}^{*} - 16/21 \cdot c_{1}^{*},$$
  

$$b_{2}^{*} = 5/21 \cdot a_{1}^{*} - 11/21 \cdot b_{1}^{*} - 20/21 \cdot c_{1}^{*},$$

$$c_2^* = -1/3 \cdot a_1^* - 2/3 \cdot b_1^* + 1/3 \cdot c_1^*$$
,  
This corresponds to a rotation through 175° about  
parallel to  $-0.334a_1 - 0.591b_1 + 0.735c_1$ . The indic

an axis ces are related by

$$h_1 = (-17 h_2 + 5 k_2 - 7 l_2)/21,$$
  

$$k_1 = (8 h_2 - 11 k_2 - 14 l_2)/21,$$

$$l_1 = (-16 h_2 - 20 k_2 + 7 l_2)/21.$$

Some reflections can be measured without overlap from the other domain, some intensities are only observed as the sum of contributions from both domains. Therefore, the sample is a non-merohedral twin. The non-overlapping reflections of one domain were sufficient to solve the structure using SHELXS [14]. For structure refinement all observed reflections from both domains were considered using the HKL 5 format in SHELXL [15], and the additional refined batch scale factor (BASF) yielded a domain ratio of 0.585:0.415.



Fig. 2. (a) Separate ReO<sub>6</sub> octahedra in the  $M_6$ ReO<sub>12</sub> (M = In, Sc) cell. Small black spheres are  $O^{2-}$  ions, large light grey ones are  $M^{3+}$  ions. (b) ScO<sub>7</sub> or InO<sub>7</sub> polyhedra connected via edges and corners. Small black balls are O<sup>2-</sup> ions, large dark grey ones are Re<sup>+6</sup> ions.

Table 3 Positional parameters for Sc<sub>6</sub>ReO<sub>12</sub> and In<sub>6</sub>ReO<sub>12</sub>.

Atom	Site	x	у	Ζ	Occup.
Sc <sub>6</sub> ReO <sub>12</sub>					
Re	3a	0	0	0	1
Sc	18 <i>f</i>	0.2495 (2)	0.0338 (2)	0.3592 (3)	1
O(1)	18 <i>f</i>	0.1868 (8)	0.0277 (8)	0.1204 (9)	1
O(2)	18 <i>f</i>	0.2173 (7)	0.0235 (7)	0.6065 (9)	1
In <sub>6</sub> ReO <sub>12</sub>					
Re	3a	0	0	0	1
In	18f	0.2496(1)	0.0353(1)	0.3540(1)	1
O(1)	18 <i>f</i>	0.1822(4)	0.0241(4)	0.1166(4)	1
O(2)	18 <i>f</i>	0.2195(3)	0.0208(3)	0. 6051(3)	1

Table 4 Anisotropic thermal displacement parameters  $(\text{\AA}^2)$  for Sc<sub>6</sub>ReO<sub>12</sub> and In<sub>6</sub>ReO<sub>12</sub>.

Atom	$U_{11}$	$U_{22}$	$U_{33}$	$U_{12}$	$U_{13}$	$U_{23}$
Sc <sub>6</sub> ReO <sub>12</sub>						
Re	0.0033 (3)	0.0033 (3)	0.0088 (5)	0.00167 (16)	0.00000	0.00000
Sc	0.0046 (8)	0.0054 (8)	0.0083 (9)	0.0033 (6)	-0.0005(6)	-0.0013 (6)
O(1)	0.008 (3)	0.012 (3)	0.014 (4)	0.004 (2)	-0.004(3)	-0.002(3)
O(2)	0.007 (3)	0.003 (2)	0.007 (4)	0.001 (2)	0.007 (3)	0.002 (3)
In <sub>6</sub> ReO <sub>12</sub>						
Re	0.004 (1)	0.004 (1)	0.007(1)	0.002(1)	0.000	0.000
In	0.009(1)	0.008 (1)	0.009(1)	0.006 (1)	0.000(1)	-0.001(1)
O(1)	0.020 (2)	0.020 (2)	0.013 (1)	0.014 (1)	-0.009(1)	-0.005(1)
O(2)	0.006 (1)	0.007 (1)	0.008 (1)	0.001 (1)	0.000 (1)	0.000 (1)

Table 5

Selected interatomic distances (Å) for  $Sc_6ReO_{12}$  and  $In_6ReO_{12}$  compared with some for  $Sc_6WO_{12}$  and  $In_6WO_{12}$ .

$Sc_6ReO_{12}$		Sc <sub>6</sub> WO <sub>12</sub> [28]		
Re-O(1)	1.926(6) (×6)	Re–O(1)	1.90 (×6)	
Sc-O(1)	2.155 (8)	Sc-O(1)	2.20	
Sc-O(1)	2.230 (3)	Sc-O(1)	2.20	
Sc-O(1)	2.670 (6)			
Sc-O(2)	2.027 (7)	Sc-O(2)	2.00	
Sc-O(2)	2.083 (6)	Sc-O(2)	2.10	
Sc-O(2)	2.119 (4)	Sc-O(2)	2.10	
Sc-O(2)	2.173 (8)	Sc-O(2)	2.20	
In <sub>6</sub> ReO <sub>12</sub>		In <sub>6</sub> WO <sub>12</sub> [7]		
Re-O(1)	1.932 (3) (×6)	W-O(1)	1.93 (×6)	
In-O(1)	2.203 (4)	In–O(1)	2.21	
In-O(1)	2.298 (1)	In-O(1)	2.28	
In-O(1)	2.727 (3)	In-O(1)	2.77	
In-O(2)	2.066 (3)	In-O(2)	2.07	
In-O(2)	2.112 (2)	In-O(2)	2.12	
In-O(2)	2.227 (1)	In-O(2)	2.21	
In–O(2)	2.257 (3)	In–O(2)	2.24	



Fig. 3.  $MO_7$ -coordination polyhedron (M = Sc, In).

The structure of  $Sc_6ReO_{12}$  and  $In_6ReO_{12}$  represents a three-dimensional framework formed by octahedra of ReO<sub>6</sub> and monocapped  $MO_7$ -prisms (M = In, Sc) connected via edges and corners (Fig. 2a and b). Positional parameters, anisotropic thermal displacement parameters and selected interatomic distances for Sc<sub>6</sub>ReO<sub>12</sub> and In<sub>6</sub>ReO<sub>12</sub> compared with some data for Sc<sub>6</sub>WO<sub>12</sub> and



Fig. 4. Dependence of the "a" and "c" cell parameters on the ionic radius [4] of the trivalent cation for  $Ln_6ReO_{12}$  (Ln = Ho, Er, Tm, Yb, Lu) [3] and In<sub>6</sub>ReO<sub>12</sub> and Sc<sub>6</sub>ReO<sub>12</sub> (this work).

In<sub>6</sub>WO<sub>12</sub> are listed in Tables 3–5, respectively. The interatomic distances in In<sub>6</sub>WO<sub>12</sub> and In<sub>6</sub>ReO<sub>12</sub> or Sc<sub>6</sub>WO<sub>12</sub> and Sc<sub>6</sub>ReO<sub>12</sub> are very similar due to close ionic radii of W<sup>+6</sup> (0.60 Å) and Re<sup>+6</sup> (0.55 Å) [4].

ReO<sub>6</sub>-octahedra are undistorted and isolated from each other, the Re–O interatomic distance  $d_{\text{Re}-\text{O}} = 1.926 \text{ Å}$  for  $Sc_6ReO_{12}$  and 1.932 Å for  $In_6ReO_{12}$  is in good agreement with Re-O bond distances observed for other Re containing oxides with a formal rhenium oxidation state of +6:  $d_{\text{Re}-\text{O}} = 1.935 \text{ Å}$  in MnReO<sub>4</sub> [26] or  $d_{\text{Re}-\text{O}} = 1.933 \text{ Å}$  in Tm<sub>6</sub>ReO<sub>12</sub> [3]. Six Sc-O and In-O bond lengths in the MO<sub>7</sub>-polyhedra (Fig. 3) forming a prism lie in an interval of 2.027-2.230 Å for Sc and 2.066-2.298 Å for In, which agrees with average Sc-O and In-O distances in Sc- and Incontaining oxides:  $d_{Sc-O} = 2.12 \text{ Å}$  for ScO<sub>6</sub>-octahedra in  $Sc_2O_3$  [27] or  $d_{Sc-O} = 2.13$  Å for  $ScO_6$  in  $Sc_6WO_{12}$  [28] and  $d_{\text{In-O}} = 2.191 \text{ Å}$  for InO<sub>6</sub>-octahedra in In<sub>2</sub>O<sub>3</sub> [29] or  $d_{\text{In-O}} = 2.27 \text{ Å}$  for InO<sub>7</sub> in In<sub>6</sub>WO<sub>12</sub> [7,8]. One *M*-O distance in MO<sub>7</sub> (2.675 Å for M = Sc and 2.727 Å for M =In) seems to be too long for a regular Sc–O and In–O chemical bond. Nevertheless, we included this oxygen in the coordination sphere of M due to three reasons:

1. The  $M_6 \text{ReO}_{12}$  (M = Sc, In) structure is very close to  $\text{Ln}_7\text{O}_{12}$  (Ln = Tb, Pr, Ce) [2] and  $Ln_6 \text{ReO}_{12}$  (Ln = Ho-Lu) [3]. A dependence of "a" and "c" cell parameters on the ionic radius for  $\text{Ln}_6 \text{ReO}_{12}$ ,  $\text{Sc}_6 \text{ReO}_{12}$  and  $\text{In}_6 \text{ReO}_{12}$  (Fig. 4) represents a straight line, demonstrating that all these compounds belong to the same structure type. In these compounds the  $Ln^{3+}$  ions have a capped prismatic coordination of 7 oxygen atoms with the usual Ln–O distance [3].

A model of "coordination defect" has been applied to discuss the Tb<sub>7</sub>O<sub>12</sub> structure [30]. This model considers an oxygen vacancy and six nearest neighbouring oxygen atoms as one structural unit in the close oxygen packing and is based on the defect and relaxation of the anion lattice. It is suggested that oxygen atoms in this structural unit move from ideal fluorite position toward the vacancy due to strong polarization. At the same time the repulsion between the oxygen vacancy and the metal ion has an opposite effect. In MO7-polyhedra in  $M_6 \text{ReO}_{12}$  (M = Sc, In, Ho–Lu) five O atoms are subjected to the strongest influence of the oxygen vacancy whereas two O atoms with the longest M-O distance remain unaffected. In the case of In<sub>6</sub>ReO<sub>12</sub> and first of all Sc<sub>6</sub>ReO<sub>12</sub> the repulsion between oxygen vacancy and  $M^{3+}$  ion is less in comparison with heavy 4*f*-ions Ln = Ho–Lu, which leads to the more irregular MO<sub>7</sub>-polyhedra.

- 2. The calculations based on the bond-valence model [31-33] with the bond-valence parameters for Sc–O  $R_o = 1.849$  and B = 0.37 and for In-O  $R_o = 1.902$  and B = 0.37 [31] gave an oxidation number for Sc of +2.842 and of +2.793 for In in an octahedral coordination, and +2.951 (Sc) and +2.901 (In) for the monocapped prismatic coordination. The latter values are more adequate for the chemistry of these metals.
- 3. There are more examples with long distances M–O (M = Sc, In), for example the average Sc-O distance for the ScO<sub>7</sub>-polyhedron in ScMnO<sub>3</sub> [34] is 2.40 Å and even larger as the one for the ScO<sub>7</sub>-polyhedron in Sc<sub>6</sub>ReO<sub>12</sub> (2.21 Å). The average In(2)–O distance for the InO<sub>7</sub>-polyhedron in InMnO<sub>3</sub> [35] is 2.27 Å and equal to the one for the InO<sub>7</sub>-polyhedron in In<sub>6</sub>ReO<sub>12</sub>.

The ionic radii ratios  $r(\text{Re}^{6+})/r(\text{Sc}^{3+})$  and  $r(\text{Re}^{6+})/r(\text{In}^{3+})$  [4] are equal to 0.73 and 0.69, respectively, in agreement with the empirical criterion for the formation of the Ln<sub>6</sub>MO<sub>12</sub> phases with rhombohedral structure as proposed in [2] for the systems  $Ln_2\text{O}_3$ –MoO<sub>3</sub>,  $Ln_2\text{O}_3$ –WO<sub>3</sub> and  $Ln_2\text{O}_3$ –UO<sub>3</sub>.

#### 3.4. Magnetic properties of $In_6ReO_{12}$ and $Sc_6ReO_{12}$

The temperature dependence of inverse magnetization of  $Sc_6ReO_{12}$  is shown in Fig. 5. At low temperature a maximum of magnetization is observed at T = 1.89(2) K (see inset). No significant difference between FC and ZFC

data is detected. A magnetic moment of  $0.65(1)\mu_B$  per Re-ion is calculated from the Curie constant in the paramagnetic region, obtained from fitting Eq. (4) to the



Fig. 5. Temperature dependence of magnetization (inset) and its inverse for  $Sc_6ReO_{12}$ .



Fig. 6. (a) Temperature dependence of the inverse specific magnetic susceptibility of  $In_6ReO_{12}$ , measured in field-cooled (FC) mode. The dashed line represents a fit according to Eq. (4). (b) Comparison of magnetization data of  $In_6ReO_{12}$ , measured in field-cooled (FC) and zero-field cooled (ZFC) mode, respectively. In the marked region, the coercivity field becomes close to the applied field strength of 500 G, and the difference between FC and ZFC data is already considerably reduced below  $T_{\rm C}$ .

Table 6 Magnetic properties of Sc<sub>6</sub>ReO<sub>12</sub> and In<sub>6</sub>ReO<sub>12</sub>

Compound	$M_0 \text{ (emu/g)}$	Θ (K)	$\mu(\mathrm{Re}^{+6})~(\mu_{\mathrm{B}})$	Temperature range for fit, K
$Sc_6ReO_{12}$	$\begin{array}{c} 4.56(8)\times 10^{-4} \\ -1.24(9)\times 10^{-4} \end{array}$	-0.7(1)	0.65(1)	10–200
$In_6ReO_{12}$		-3.2(3)	0.84(1)	15–100

The standard deviations in brackets are determined as the limits, for which an up to 10% higher residual is obtained in the least-square fit than for the optimum fit for Eq. (4).



Fig. 7. (a) Hysteresis loop of  $In_6ReO_{12}$ , measured at 4.5 K. (b) Low-field section of the hysteresis loop of  $In_6ReO_{12}$ , measured at 4.5 K.

observed data.

$$M(T) = \frac{C}{T - \theta} + M_0. \tag{4}$$

This value is similar to those for other compounds with  $\text{Re}^{+6}$  (5 $d^1$  electron configuration), for example 0.74  $\mu_B$  in  $Lu_6\text{ReO}_{12}$  [3] and 0.80  $\mu_B$  in  $\text{Sr}_{11}\text{Re}_4\text{O}_{24}$  [36]. A maximum in the temperature dependence of magnetization was also observed for the isostructural compound Yb<sub>6</sub>ReO<sub>12</sub> at 2.15(10) K [3]. Additional neutron diffraction and magnetization studies at least down to 1.5 K are required to distinguish antiferromagnetic ordering from a spin-glass behaviour. The close values for the temperatures with

maximum magnetization for  $Sc_6ReO_{12}$  and  $Yb_6ReO_{12}$  give evidence that the underlying effect is not dominated by the more and larger  $Yb^{3+}$  magnetic moments, but due to interactions within the  $Re^{+6}$ -sublattice.

In<sub>6</sub>ReO<sub>12</sub> reveals a pronounced increase of magnetization below  $T_{\rm C} = 7.5(5)$  K, shown as an abrupt decrease in the inverse specific susceptibility  $\chi_{\rm m}^{-1}$  in Fig. 6a. A magnetic moment of  $0.84(1)\mu_B$  per Re-ion is deduced from the paramagnetic region according to Eq. (4) with the parameters from Table 6. A ferromagnetic component is confirmed by the difference in magnetizations below  $T_{\rm C}$ for data collection in FC and ZFC mode, see Fig. 6b. In the marked region between 4 and 6K the zero-field cooled magnetization data approach successively those measured in field-cooled mode. This behaviour reflects the temperature dependence of the coercivity field  $H_{\rm C}(T)$ , which becomes in this temperature region close to or lower than the applied field strength of 500 G. At 4.5 K the coercivity field is determined to about 250G from the corresponding hysteresis loop, see Fig. 7(a) for the complete loop and Fig. 7(b) for the low-field region. The appearance of ferromagnetism in In<sub>6</sub>ReO<sub>12</sub> is rather surprising in the light of the more negative Curie-Weiss temperature  $\theta$  than for Sc<sub>6</sub>ReO<sub>12</sub> and the nearest Re–Re distance of more than 6Å. A possible mechanism might be based on an insulator to metal transition from  $\operatorname{Re}^{+6}$  ions into  $\operatorname{Re}^{+7}$  cores plus itinerant electrons. Note that a similar magnetic behaviour is also observed for  $Sr_{11}Re_4O_{24}$  with  $Re^{+6}$  and  $Re^{+7}$  ions, which orders with a ferromagnetic component below the Curie temperature of  $T_{\rm C} = 12(1) \, {\rm K}$  [36].

#### Acknowledgments

The authors are indebted to T. Kautz (Institut fuer Geowissenschaften, Johann Wolfgang Goethe Universitaet Frankfurt am Main, Germany) for help by performing the high-pressure high-temperature synthesis experiments. Financial support by the Deutsche Forschungsgemeinschaft (DFG FU125/42) is gratefully acknowledged.

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